

# Cambridge International AS & A Level

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**MATHEMATICS****9709/15**

Paper 1 Pure Mathematics 1

**May/June 2026****MARK SCHEME**Maximum Mark: 75

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**Published**

This mark scheme contains the instructions and marking guidance that our examiners used to mark candidate responses for this component.

Before they start marking, examiners complete a standardisation process. They review a range of candidate responses and discuss the mark scheme in detail to agree which answers can and cannot be accepted. Examiners award marks where it is clear that candidate responses have met the requirements of the mark scheme. These requirements may vary between different components or different versions of the same component, depending on the exact requirements of the question and the candidate responses seen during the standardisation process.

Sometimes, our mark schemes may allow marks to be awarded to responses which contain elements that are factually incorrect or for content not covered by the syllabus. We do this in response to the demands of a specific question to support candidates and make sure that our assessments are fair. However, these allowances should not be used as a guide for teaching and learning.

We cannot discuss the mark scheme with schools, and we recommend that schools read the mark scheme together with the assessment material and the Principal Examiner Report for Teachers.

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This document consists of **21** printed pages.

**General marking principles**

All examiners must apply these marking principles when marking candidate responses.

|   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|---|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1 | Examiners must award marks for each response in line with: <ul style="list-style-type: none"><li>the specific <b>content</b> defined in the mark scheme</li><li>the specific <b>skills</b> defined in the mark scheme or in the level descriptions</li><li>the <b>standard of response</b> required as exemplified by the standardisation scripts.</li></ul>                                                                                                                                                                                                                                                                                    |
| 2 | Examiners must award <b>whole marks</b> (not half marks, or other fractions).                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
| 3 | Examiners must award marks <b>positively</b> . This means that: <ul style="list-style-type: none"><li>marks are not deducted for errors or omissions</li><li>marks are awarded for correct/valid answers as defined in the mark scheme and also for <b>other valid answers</b> which go beyond the scope of the syllabus and mark scheme referring to your team leader as appropriate</li><li>the quality of spelling, punctuation and grammar are judged <b>only</b> when the mark scheme indicates that these features are <b>specifically assessed</b> in the question. However, the meaning of all responses must be unambiguous.</li></ul> |
| 4 | Examiners must <b>consistently</b> apply the requirements of the mark scheme and any rules for what to do when candidates have not followed instructions correctly.                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
| 5 | Examiners must use the <b>full range of marks</b> defined in the mark scheme, unless limited by the quality of the candidate responses seen.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| 6 | Examiners must award marks according to the mark scheme and <b>must not</b> award marks with grade thresholds or grade descriptions in mind.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |

**Mathematics-Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

**Annotations guidance for centres**

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

**Annotations**

| <b>Annotation</b>                                                                   | <b>Meaning</b>                         |
|-------------------------------------------------------------------------------------|----------------------------------------|
|    | More information required              |
|    | Accuracy mark awarded zero             |
|    | Accuracy mark awarded one              |
|    | Independent accuracy mark awarded zero |
|  | Independent accuracy mark awarded one  |
|  | Independent accuracy mark awarded two  |
|  | Benefit of the doubt                   |
|  | Blank Page                             |
|  | Incorrect                              |
| Dep                                                                                 | Used to indicate DM0 or DM1            |

| <b>Annotation</b>                                                                   | <b>Meaning</b>                                                                                                                             |
|-------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| DM1                                                                                 | Dependent on the previous M1 mark(s)                                                                                                       |
|    | Follow through                                                                                                                             |
|    | Indicate working that is right or wrong                                                                                                    |
| Highlighter                                                                         | Highlight a key point in the working                                                                                                       |
|    | Ignore subsequent work                                                                                                                     |
|    | Judgement                                                                                                                                  |
|    | Judgement                                                                                                                                  |
|    | Method mark awarded zero                                                                                                                   |
|    | Method mark awarded one                                                                                                                    |
|    | Method mark awarded two                                                                                                                    |
|    | Misread                                                                                                                                    |
|    | Omission or Other solution                                                                                                                 |
| Off-page comment                                                                    | Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to. |
| On-page comment                                                                     | Allows comments to be entered in speech bubbles on the candidate response.                                                                 |
|  | Judgment made by the PE                                                                                                                    |
|  | Premature approximation                                                                                                                    |
|  | Special case                                                                                                                               |
|  | Indicates that work/page has been seen                                                                                                     |

| Annotation                                                                        | Meaning                                |
|-----------------------------------------------------------------------------------|----------------------------------------|
| <b>SF</b>                                                                         | Error in number of significant figures |
|  | Correct                                |
| <b>TE</b>                                                                         | Transcription error                    |
| <b>XP</b>                                                                         | Correct answer from incorrect working  |

**PUBLISHED****Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

**Types of mark**

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
  - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
  - The total number of marks available for each question is shown at the bottom of the Marks column.
  - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
  - Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

**Abbreviations**

|        |                                                                                                                                                                                       |
|--------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AEF/OE | Any Equivalent Form (of answer is equally acceptable) / Or Equivalent                                                                                                                 |
| AG     | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)                                                   |
| CAO    | Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)                                                                                           |
| CWO    | Correct Working Only                                                                                                                                                                  |
| ISW    | Ignore Subsequent Working                                                                                                                                                             |
| SOI    | Seen Or Implied                                                                                                                                                                       |
| SC     | Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |
| WWW    | Without Wrong Working                                                                                                                                                                 |
| AWRT   | Answer Which Rounds To                                                                                                                                                                |

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| Question | Answer                                                                                                                                        | Marks        | Guidance                                                                                                                                |
|----------|-----------------------------------------------------------------------------------------------------------------------------------------------|--------------|-----------------------------------------------------------------------------------------------------------------------------------------|
| 1        | <b>EITHER</b><br>Solution 1<br>$2x = y + 5$ so $(y + 5)^2 + 2y^2 - 3y = 21$                                                                   | <b>(M1)*</b> | For rearranging and substituting/eliminating $x$ .                                                                                      |
|          | $3y^2 + 7y + 4 = 0$                                                                                                                           | <b>DM1</b>   | For forming a three-term quadratic.                                                                                                     |
|          | $(3y + 4)(y + 1) = 0$                                                                                                                         | <b>DM1</b>   | For attempt to solve using factorisation, quadratic formula or completing the square. <i>Their</i> quadratic must have a real solution. |
|          | $y = -\frac{4}{3}$ and $y = -1$                                                                                                               | <b>A1</b>    | If one coordinate correct, award A1.<br>Both A marks are dependent on the first two M marks only.                                       |
|          | $x = \frac{11}{6}$ and $x = 2$                                                                                                                | <b>A1)</b>   | If the other coordinate is correct, award this A1.                                                                                      |
|          | <b>OR</b><br>Solution 2<br><b>Alternative Method for Question 1: Substituting for <math>y</math></b><br>$4x^2 + 2(2x - 5)^2 - 3(2x - 5) = 21$ | <b>(M1)*</b> | For rearranging and substituting/eliminating $y$ .                                                                                      |
|          | $12x^2 - 46x + 44 = 0$                                                                                                                        | <b>DM1</b>   | For forming a three-term quadratic.                                                                                                     |
|          | $2(x - 2)(6x - 11) = 0$                                                                                                                       | <b>DM1</b>   | For attempt to solve using factorisation, quadratic formula or completing the square. <i>Their</i> quadratic must have a real solution. |
|          | $x = \frac{11}{6}$ and $x = 2$                                                                                                                | <b>A1</b>    | If one coordinate is correct, award this A1.<br>Both A marks are dependent on the first two M marks only.                               |
|          | $y = -\frac{4}{3}$ and $y = -1$                                                                                                               | <b>A1)</b>   | If the other coordinate is correct, award this A1.                                                                                      |
|          |                                                                                                                                               | <b>5</b>     |                                                                                                                                         |

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| Question | Answer                                                                                  | Marks     | Guidance                                                                                                                                                  |
|----------|-----------------------------------------------------------------------------------------|-----------|-----------------------------------------------------------------------------------------------------------------------------------------------------------|
| 2        | $\left[ \frac{dV}{dh} = \right] 100\pi + \pi h^2 \quad [=1000\pi \text{ when } h = 30]$ | <b>B1</b> |                                                                                                                                                           |
|          | $\frac{dh}{dt} = \frac{200}{\text{their } \frac{dV}{dh}}$                               | <b>M1</b> | OE, for correct use of chain rule with <i>their</i> $\frac{dV}{dh}$ at $h = 30$ .<br>May be implied by a correct final answer or $\frac{dt}{dh} = 5\pi$ . |
|          | $\left[ \frac{dh}{dt} = \right] \frac{200}{1000\pi} \left[ = \frac{1}{5\pi} \right]$    | <b>A1</b> | OE, must be exact.<br>0.064 is A0.                                                                                                                        |
|          |                                                                                         | <b>3</b>  |                                                                                                                                                           |

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| Question | Answer                                                             | Marks     | Guidance                                                                                                                                               |
|----------|--------------------------------------------------------------------|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------|
| 3(a)     | $5 \times p \times 2^4$ or $6 \times 1^2 \times (-2q)^2$           | <b>B1</b> | For either expansion, expect $80p$ and $24q^2$ .<br>Allow terms in $x$ here.<br>Allow if seen to be correct in an expansion with other terms.          |
|          | $5 \times p \times 2^4 = 6 \times 1^2 \times (-2q)^2$              | <b>M1</b> | For forming equation from <i>their</i> two terms providing each comes from a term in $x^4$ and $x^2$ . Do not allow $x$ in either term.                |
|          | $p = \frac{3}{10}q^2$                                              | <b>A1</b> | OE, $p$ must be the subject of <i>their</i> expression.                                                                                                |
|          |                                                                    | <b>3</b>  |                                                                                                                                                        |
| 3(b)     | $p = \frac{6}{5} \Rightarrow q = \pm 2$                            | <b>B1</b> |                                                                                                                                                        |
|          | Coefficient of $x^3$ is $20 \times 3^3 \times (\text{their } q)^3$ | <b>M1</b> | Allow $x^3$ here.<br>If the expansion is given, this term must be selected.<br><i>Their</i> $q$ may be in terms of $p$ but must not contain $x$ terms. |
|          | $\pm 4320$                                                         | <b>A1</b> | Must be coefficients only.                                                                                                                             |
|          |                                                                    | <b>3</b>  |                                                                                                                                                        |

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| Question | Answer                                                         | Marks       | Guidance                                                                                                                                                    |
|----------|----------------------------------------------------------------|-------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 4(a)     | $\left[ \frac{dy}{dx} = \right] -8x + 2$                       | <b>B1*</b>  | Must use differentiation.                                                                                                                                   |
|          | $\left[ \frac{dy}{dx} = 0 \Rightarrow \right] x = \frac{1}{4}$ | <b>DB1</b>  | OE, allow 0.25.                                                                                                                                             |
|          |                                                                | <b>2</b>    |                                                                                                                                                             |
| 4(b)     | $\frac{1}{8}$                                                  | <b>B1FT</b> | OE, allow 0.125.<br>Half of <i>their</i> $x$ coordinate. Ignore $y$ -values.                                                                                |
|          |                                                                | <b>1</b>    |                                                                                                                                                             |
| 4(c)     | $[y =] 3(-4 \times (2x)^2 + 2 \times (2x) + 3)$ or             | <b>M1</b>   | M1 for stretch in $y$ -direction with RHS multiplied by 3 in <i>their</i> $y$ .                                                                             |
|          | $[y =] 3(-4(2x - \frac{1}{4})^2 + \frac{13}{4})$               | <b>M1</b>   | M1 for stretch in $x$ -direction, $x$ replaced by $2x$ using <i>their</i> $y$ .<br><i>Their</i> $y$ could be an incorrect attempt at completing the square. |
|          | $y = -48x^2 + 12x + 9$                                         | <b>A1</b>   | Allow 'f(x) ='.<br>If subject of the formula missing throughout, then A0.<br>Allow $a = -48$ , $b = 12$ , $c = 9$ .                                         |
|          |                                                                | <b>3</b>    |                                                                                                                                                             |

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| Question | Answer                                                      | Marks         | Guidance                                                                             |
|----------|-------------------------------------------------------------|---------------|--------------------------------------------------------------------------------------|
| 5(a)     | $2(x-4)^2 - 50$                                             | <b>B2,1,0</b> | B2 no errors, B1 one error, B0 more than one error.                                  |
|          |                                                             | <b>2</b>      |                                                                                      |
| 5(b)     | $2(x^4 - 4)^2 - 50 = 0 \quad [\Rightarrow x^4 - 4 = \pm 5]$ | <b>M1*</b>    | Replacing $x$ by $x^4$ in <i>their</i> completed square form.                        |
|          | $x^4 = 9 \quad [\text{or } x^4 = -1]$                       | <b>B1</b>     | May be implied by a substitution for $x^4$ .                                         |
|          | $x = [\pm] \sqrt[4]{9}$                                     | <b>DM1</b>    | For finding the 4th root of <i>their</i> 9.<br>May be implied by $\sqrt{3}$ or 1.73. |
|          | $x = \pm\sqrt{3}$                                           | <b>B1</b>     | B0 for final answer in non-surd form.                                                |
|          |                                                             | <b>4</b>      |                                                                                      |

| Question | Answer                                                                    | Marks      | Guidance                                                                                                                                                                      |
|----------|---------------------------------------------------------------------------|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 6        | $4 - 7x - 2x^2 = k - 4x$                                                  | <b>M1*</b> | For equating.                                                                                                                                                                 |
|          | $\pm(2x^2 + 3x + k - 4)[= 0]$                                             | <b>A1</b>  |                                                                                                                                                                               |
|          | $9 - 4 \times 2 \times (k - 4) \geq 0 \quad [\Rightarrow 8k \leq 9 + 32]$ | <b>DM1</b> | For use of $b^2 - 4ac \geq 0$ correctly for <i>their</i> $a$ , $b$ and $c$ .<br>May be seen as $b^2 - 4ac > 0$ <b>and</b> $b^2 - 4ac = 0$ , but the results must be combined. |
|          | $k \leq \frac{41}{8}$                                                     | <b>A1</b>  | OE<br>Accept $k \leq 5.125$ , must be the final answer.                                                                                                                       |
|          |                                                                           | <b>4</b>   |                                                                                                                                                                               |

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| Question | Answer                                                                                                                                                                                                                                                                                                                                                                     | Marks | Guidance                                                                                                                                           |
|----------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|----------------------------------------------------------------------------------------------------------------------------------------------------|
| 7(a)     | $\frac{\cos \theta}{1 - \sin \theta} - \frac{1}{\cos \theta} \equiv \frac{\cos \theta \cos \theta}{(1 - \sin \theta) \cos \theta} - \frac{(1 - \sin \theta)}{(1 - \sin \theta) \cos \theta}$ or $\frac{\cos \theta(1 + \sin \theta)}{(1 - \sin \theta)(1 + \sin \theta)} - \frac{\cos \theta}{\cos^2 \theta}$                                                              | M1    | Use of common denominator may occur later in <i>their</i> proof.<br>Must prove LHS = RHS.                                                          |
|          | $\equiv \frac{1 - \sin^2 \theta - (1 - \sin \theta)}{(1 - \sin \theta) \cos \theta} \text{ or } \frac{\cos \theta + \cos \theta \sin \theta}{\cos^2 \theta} - \frac{\cos \theta}{\cos^2 \theta}$                                                                                                                                                                           | M1    | Use of $\sin^2 \theta + \cos^2 \theta \equiv 1$ .                                                                                                  |
|          | $\equiv \frac{(1 - \sin \theta)(1 + \sin \theta) - (1 - \sin \theta)}{(1 - \sin \theta) \cos \theta} \equiv \frac{(1 + \sin \theta) - 1}{\cos \theta}$ or $\frac{-\sin^2 \theta + \sin \theta}{(1 - \sin \theta) \cos \theta} \equiv \frac{(1 - \sin \theta) \sin \theta}{(1 - \sin \theta) \cos \theta}$ or $\frac{1 + \sin \theta}{\cos \theta} - \frac{1}{\cos \theta}$ | M1    | For simplifying.                                                                                                                                   |
|          | $\equiv \tan \theta$                                                                                                                                                                                                                                                                                                                                                       | A1    | WWW or any incorrect notation.<br>Accept any valid alternative method.                                                                             |
|          |                                                                                                                                                                                                                                                                                                                                                                            | 4     |                                                                                                                                                    |
| 7(b)     | $2 \tan \theta + 3 = 0$                                                                                                                                                                                                                                                                                                                                                    | B1    | OE                                                                                                                                                 |
|          | $\theta = \tan^{-1} \left( -\frac{3}{2} \right)$ or $-56.3^\circ$ or $123.7^\circ$ or $303.7^\circ$                                                                                                                                                                                                                                                                        | M1    | For solving <i>their</i> equation in $\tan \theta$ . If <i>their</i> equation is incorrect, must see answer in the form $\theta = \tan^{-1} \dots$ |
|          | $\theta = 123.7^\circ$ and $303.7^\circ$ only                                                                                                                                                                                                                                                                                                                              | A1    | AWRT 123.7 and 303.7.                                                                                                                              |
|          |                                                                                                                                                                                                                                                                                                                                                                            | 3     |                                                                                                                                                    |

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| Question | Answer                                                                                                                                                                  | Marks     | Guidance                                                                                                  |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|-----------------------------------------------------------------------------------------------------------|
| 8(a)     | $\left[ QR = 5a \tan\left(\frac{1}{6}\pi\right) = \frac{5}{3}\sqrt{3}a \right] \quad QS = \sqrt{\left(5a \tan\left(\frac{1}{6}\pi\right)\right)^2 + a^2}$               | <b>M1</b> | OE. A correct method for finding an expression for $QS$ or $QS^2$ .<br>Allow M1 for decimal calculations. |
|          | $QS = \sqrt{\frac{28}{3}}a$                                                                                                                                             | <b>A1</b> | Accept $\sqrt{\frac{84}{9}}a$ .                                                                           |
|          |                                                                                                                                                                         | <b>2</b>  |                                                                                                           |
| 8(b)(i)  | $\sin RQS = \frac{a}{\text{their} \sqrt{\frac{28}{3}}a}$                                                                                                                | <b>M1</b> | Award for use of <i>their QS</i> , providing <i>their QS</i> > $a$ .                                      |
|          | $[RQS =] \sin^{-1}\left(\frac{\sqrt{21}}{14}\right)$                                                                                                                    | <b>A1</b> | AG, must show convincing reasoning for $\frac{a}{\sqrt{\frac{28}{3}}a} = \frac{\sqrt{21}}{14}$ .          |
|          |                                                                                                                                                                         | <b>2</b>  |                                                                                                           |
| 8(b)(ii) | $\left[ \theta = \pi - \frac{\pi}{6} - \frac{\pi}{2} - \sin^{-1}\left(\frac{\sqrt{21}}{14}\right) = \right] \frac{\pi}{3} - \sin^{-1}\left(\frac{\sqrt{21}}{14}\right)$ | <b>B1</b> | Or from sine rule, $[\theta =] \sin^{-1} \sqrt{\frac{3}{7}}$ , OE.                                        |
|          |                                                                                                                                                                         | <b>1</b>  |                                                                                                           |

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| Question | Answer                                                                                                                                     | Marks         | Guidance                                                                                                 |
|----------|--------------------------------------------------------------------------------------------------------------------------------------------|---------------|----------------------------------------------------------------------------------------------------------|
| 9(a)(i)  | $-(-1) \times 4 \times 2(2x+3)^{-2} \left[ = 8(2x+3)^{-2} \right]$                                                                         | <b>B2,1,0</b> | B2 no errors, B1 one error, B0 more than one error.                                                      |
|          |                                                                                                                                            | <b>2</b>      |                                                                                                          |
| 9(a)(ii) | $(2x+3)^{-2} > 0$ or $(2x+3) > 0$ or $(2x+3)^2 > 0$<br>and<br>$f'(x) > 0$ or $k(2x+3)^{-2} > 0$                                            | <b>B1FT</b>   | Follow through on positive values of $k$ .<br>Cannot be gained by substituting exemplar values for $x$ . |
|          |                                                                                                                                            | <b>1</b>      |                                                                                                          |
| 9(b)(i)  | $\frac{4}{3-y} = 2x+3$ or $y(2x+3) = 3(2x+3) - 4$                                                                                          | <b>M1</b>     | $2x+3$ or $2y+3$ moved into the numerator.<br>$x, y$ may be interchanged.                                |
|          | Making $x$ the subject (or $y$ if interchanged).                                                                                           | <b>M1</b>     |                                                                                                          |
|          | $f^{-1}(x) = \frac{2}{3-x} - \frac{3}{2}$ or $f^{-1}(x) = \frac{1}{2} \left( \frac{4}{3-x} - 3 \right)$ or $f^{-1}(x) = \frac{5-3x}{2x-6}$ | <b>A1</b>     | OE, denominator and numerator cannot be fractions.<br>Allow ' $y =$ ' or ' $f^{-1} =$ '.                 |
|          |                                                                                                                                            | <b>3</b>      |                                                                                                          |
| 9(b)(ii) | [Domain is] $x < 3$                                                                                                                        | <b>B1</b>     | Allow correct set notation.                                                                              |
|          | [Range is] $f^{-1}(x) > -\frac{3}{2}$                                                                                                      | <b>B1</b>     | Allow $y > -\frac{3}{2}$ or $f^{-1} > -\frac{3}{2}$ .<br>Allow correct set notation.                     |
|          |                                                                                                                                            | <b>2</b>      |                                                                                                          |

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| Question | Answer                                                                                                                                                                                                                                                                                                                                                                                                                   | Marks      | Guidance                                                                                                                                                                                                                                                                                                                                   |
|----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 10       | $x^2 - 12x + 37 = -4x + 30 \Rightarrow x^2 - 8x + 7 [= 0]$                                                                                                                                                                                                                                                                                                                                                               | <b>M1</b>  | Reaching a three-term quadratic equation.<br>May be implied by sight of solutions 7 and 1.                                                                                                                                                                                                                                                 |
|          | $(x-1)(x-7)[= 0] \rightarrow x=1 \text{ or } x=7$                                                                                                                                                                                                                                                                                                                                                                        | <b>A1</b>  | Answers without any working M0A0.                                                                                                                                                                                                                                                                                                          |
|          | $[\text{Area} =] \int_1^7 ((-4x+30) - (x^2-12x+37)) dx \left[ = \int_1^7 (-x^2+8x-7) dx \right]$ $\text{or } \int_1^7 (-4x+30) dx - \int_1^7 (x^2-12x+37) dx$ $\text{or their } \frac{1}{2}(26+2)(7-1) - \int_1^7 (x^2-12x+37) dx$                                                                                                                                                                                       | <b>M1</b>  | Correct expression for the required area using <i>their</i> 1 and <i>their</i> 7.<br>May be awarded later.<br><br><i>Their</i> area of trapezium – area under the curve.                                                                                                                                                                   |
|          | $= \left[ -\frac{1}{3}x^3 + 4x^2 - 7x \right]_1^7$ $\text{or } \left[ -\frac{4}{2}x^2 + 30x \right]_1^7 \text{ and } \left[ \frac{1}{3}x^3 - 6x^2 + 37x \right]_1^7$ $\text{or } 84 \text{ and } \left[ \frac{1}{3}x^3 - 6x^2 + 37x \right]_1^7$                                                                                                                                                                         | <b>M1*</b> | For integrating (limits not needed). Only need to see one term integrated correctly in the quadratic expression for the M1.                                                                                                                                                                                                                |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                          | <b>A1</b>  |                                                                                                                                                                                                                                                                                                                                            |
|          | $\left( -\frac{1}{3}(7^3) + 4 \times 7^2 - 7 \times 7 \right) - \left( -\frac{1}{3}(1^3) + 4 \times 1^2 - 7 \times 1 \right)$ $\text{or } (-2(7^2) + 30(7)) - (-2 + 30) \text{ and}$ $\left( \frac{1}{3}(7^3) - 6(7^2) + 37(7) \right) - \left( \frac{1}{3} - 6 + 37 \right)$ $\text{or their } 84 \text{ and } \left\{ \left( \frac{1}{3}(7^3) - 6(7^2) + 37(7) \right) - \left( \frac{1}{3} - 6 + 37 \right) \right\}$ | <b>DM1</b> | For substituting <i>their</i> limits (from the initial quadratic solution).<br>Allow one slip in the substitution of limits, allow decimals.<br>Minimum required: $\frac{98}{3} - \left(-\frac{10}{3}\right)$<br>or $112 - 28 \text{ and } \frac{238}{3} - \frac{94}{3}$<br>or <i>their</i> $84 \text{ and } \frac{238}{3} - \frac{94}{3}$ |
|          | 36                                                                                                                                                                                                                                                                                                                                                                                                                       | <b>A1</b>  | WWW, dependent on the M1*.                                                                                                                                                                                                                                                                                                                 |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                          | <b>7</b>   |                                                                                                                                                                                                                                                                                                                                            |

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| Question | Answer                                                                                                                                                                                   | Marks       | Guidance                                     |
|----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|----------------------------------------------|
| 11(a)    | <b>EITHER</b><br>At $A$ , $(x-6)^2 + (2x+1-3)^2 = 20$ , $x^2 - 12x + 36 + 4x^2 - 8x + 4 = 20$<br>or At $B$ ,<br>$(x-6)^2 + (-2x+25-3)^2 = 20$ , $x^2 - 12x + 36 + 4x^2 - 88x + 484 = 20$ | <b>(M1*</b> | For substituting and expanding the brackets. |
|          | $5x^2 - 20x + 20 = 0 \rightarrow 5(x-2)(x-2) = 0$ or<br>$5x^2 - 100x + 500 = 0 \rightarrow 5(x-10)(x-10) = 0$                                                                            | <b>M1</b>   | For factorising or other solution methods.   |
|          | $A$ is (2, 5) or $B$ is (10, 5).                                                                                                                                                         | <b>DB1</b>  | Dependent only on the first M1.              |
|          | $[5 = -2x + 25 \Rightarrow] B$ is (10, 5) or $[5 = 2x + 1 \Rightarrow] A$ is (2, 5).                                                                                                     | <b>B1)</b>  | For a correct second coordinate.             |
|          | <b>OR</b> Gradient of $AC = -\frac{1}{2}$ , equation of $AC$ is $y - 3 = -\frac{1}{2}(x - 6)$ .                                                                                          | <b>(M1*</b> | OE, for example may start by finding $B$ .   |
|          | Solve with tangent at $A$ .                                                                                                                                                              | <b>M1</b>   |                                              |
|          | $A$ is (2, 5)                                                                                                                                                                            | <b>DB1</b>  | May start with $B$ being found.              |
|          | $B$ is (10, 5).                                                                                                                                                                          | <b>B1)</b>  |                                              |
|          | <b>OR</b><br>Any point on tangent at $A$ is $(x, 2x + 1)$ .<br>Gradient of $AC = -\frac{1}{2}$ , $C$ is (6, 3).                                                                          | <b>(M1*</b> | OE, for example may start by finding $B$ .   |
|          | $\frac{2x+1-3}{x-6} = -\frac{1}{2}$                                                                                                                                                      | <b>M1</b>   |                                              |
|          | $A$ is (2, 5).                                                                                                                                                                           | <b>DB1</b>  | May start with $B$ being found.              |
|          | $B$ is (10, 5).                                                                                                                                                                          | <b>B1)</b>  |                                              |
|          |                                                                                                                                                                                          | <b>4</b>    |                                              |

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| Question | Answer                                                                                                                                                                    | Marks     | Guidance                                                                                                                                                                                                                       |
|----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 11(b)    | Centre of circle is (6,3) or radius = $\sqrt{20}$                                                                                                                         | <b>B1</b> | SOI                                                                                                                                                                                                                            |
|          | Angle at centre is<br>$2 \tan^{-1}\left(\frac{4}{2}\right)$ or $2 \sin^{-1}\left(\frac{4}{\sqrt{20}}\right)$ or $2 \cos^{-1}\left(\frac{2}{\sqrt{20}}\right)$ or 2.21[42] | <b>B1</b> | Allow 126.87° if degrees used to find the two areas.<br>Other methods may be used.                                                                                                                                             |
|          | Area of sector = $\frac{1}{2} \times (\sqrt{20})^2 \times \text{their } 2.2142\dots$ [= 22.142...]                                                                        | <b>M1</b> | For area of minor sector, may be seen as difference between area of circle and area of major sector.<br>M2 for correct use of the segment formula $A = \frac{1}{2}r^2(\theta - \sin \theta)$ .<br><i>Their</i> 2.214 < $\pi$ . |
|          | Area of triangle = $\frac{1}{2} \times 8 \times 2$ or $\frac{1}{2} \times (\sqrt{20})^2 \times \sin(\text{their } 2.2142\dots)$ [= 8]                                     | <b>M1</b> | For area of triangle. <i>Their</i> 2.214 < $\pi$ .                                                                                                                                                                             |
|          | Segment area = 14.1                                                                                                                                                       | <b>A1</b> | May use circle area – major sector area – triangle area.                                                                                                                                                                       |
|          |                                                                                                                                                                           | <b>5</b>  |                                                                                                                                                                                                                                |

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| Question | Answer                                                                                                     | Marks     | Guidance                                                                                                                         |
|----------|------------------------------------------------------------------------------------------------------------|-----------|----------------------------------------------------------------------------------------------------------------------------------|
| 12(a)    | $5730 - 23(n-1) = 0$ or $\leq 0$ or $< 0 [\Rightarrow n = 250.1\dots]$                                     | <b>M1</b> | OE, for attempt to find $n$ , may not see use of arithmetic progression formula.                                                 |
|          | $5730 - 23(251-1)$                                                                                         | <b>M1</b> | OE, for attempt to find correct term.                                                                                            |
|          | -20                                                                                                        | <b>A1</b> | This must be stated or implied to be the required term.<br>SC B1 for answer only or no relevant working with the correct answer. |
|          |                                                                                                            | <b>3</b>  |                                                                                                                                  |
| 12(b)(i) | $\left[ r = \frac{\frac{1}{2} \tan \theta}{\sin \theta} = \right] \frac{1}{2 \cos \theta}$                 | <b>B1</b> | For common ratio.                                                                                                                |
|          | $\frac{1}{2 \cos \theta} < 1 \Rightarrow \cos \theta > \frac{1}{2}$ (ignore $\cos \theta < -\frac{1}{2}$ ) | <b>M1</b> | For reaching a correct inequality in $\cos \theta$ .                                                                             |
|          | $0 < \theta < \frac{1}{3} \pi$                                                                             | <b>A1</b> | Condone an answer of $\theta < \frac{1}{3} \pi$ as the lower boundary of the range is given.                                     |
|          |                                                                                                            | <b>3</b>  |                                                                                                                                  |

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| Question  | Answer                                                                                                                                                                                                                          | Marks      | Guidance                                                                                                                                       |
|-----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|------------------------------------------------------------------------------------------------------------------------------------------------|
| 12(b)(ii) | $\left[ S_{\infty} = \frac{\sin \theta}{1 - \frac{1}{2 \cos \theta}} \right] = \frac{\sin\left(\frac{1}{6}\pi\right)}{1 - \frac{1}{2 \cos\left(\frac{1}{6}\pi\right)}} \text{ or } \frac{\frac{1}{2}}{1 - \frac{1}{3}\sqrt{3}}$ | <b>M1*</b> | For use of formula.<br>$r$ may be unsimplified here as $\frac{\frac{1}{2} \tan\left(\frac{1}{6}\pi\right)}{\sin\left(\frac{1}{6}\pi\right)}$ . |
|           | $\left[ S_{\infty} = \frac{\frac{1}{2}}{1 - \frac{1}{2\left(\frac{1}{2}\sqrt{3}\right)}} = \frac{\frac{1}{2}}{\frac{3 - \sqrt{3}}{3}} = \frac{\frac{3}{2}}{3 - \sqrt{3}} \text{ or } \frac{3}{6 - 2\sqrt{3}} \right]$           | <b>DM1</b> | OE, for removing all fractions in the denominator.                                                                                             |
|           | $= \frac{\frac{3}{2}}{3 - \sqrt{3}} \times \frac{3 + \sqrt{3}}{3 + \sqrt{3}} = \frac{9 + 3\sqrt{3}}{12} = \frac{3 + \sqrt{3}}{4}$                                                                                               | <b>A1</b>  | Accept all integer equivalents, for example $\frac{9 + \sqrt{27}}{12}$ .<br>Derivation from line 2 must be shown clearly.                      |
|           |                                                                                                                                                                                                                                 | <b>3</b>   |                                                                                                                                                |